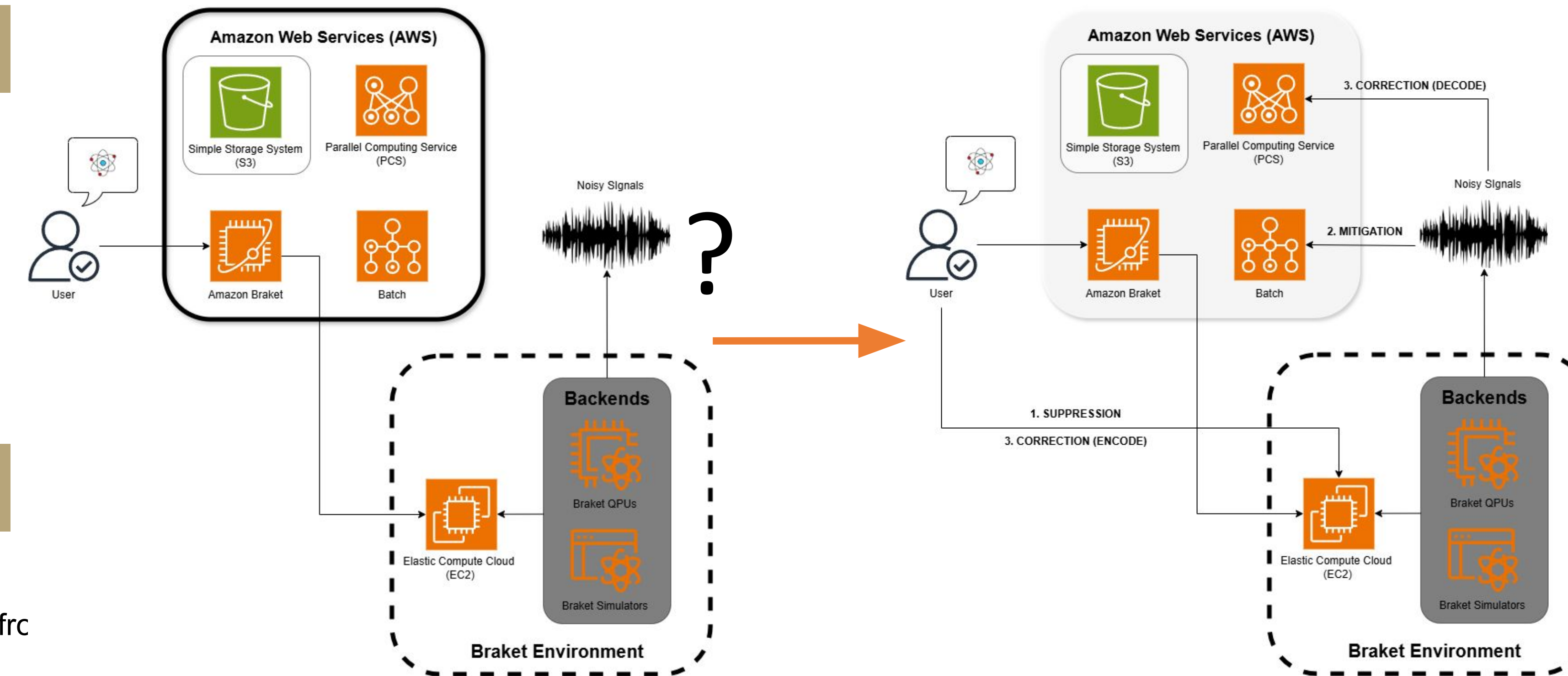
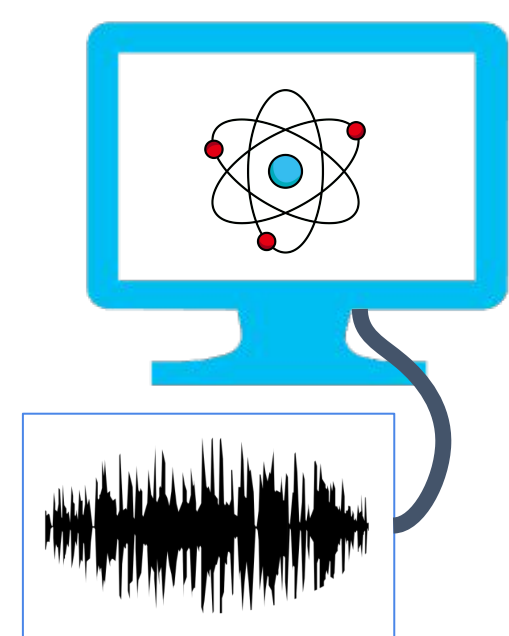


## Motivation and Background

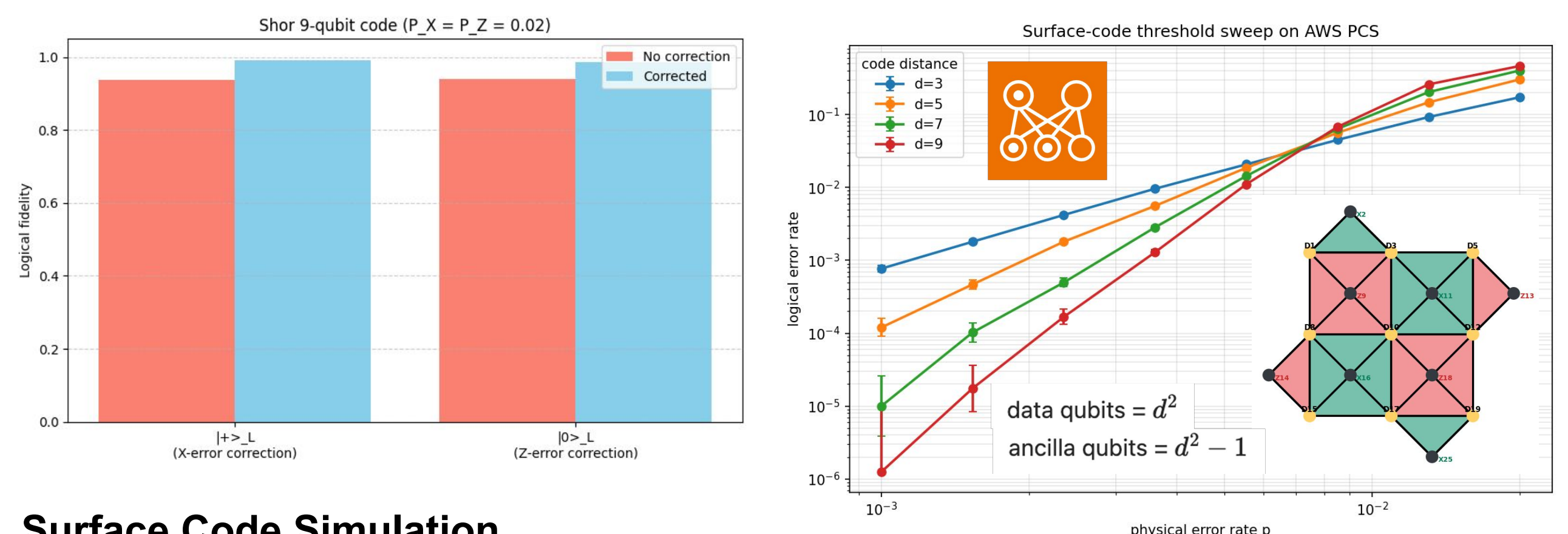
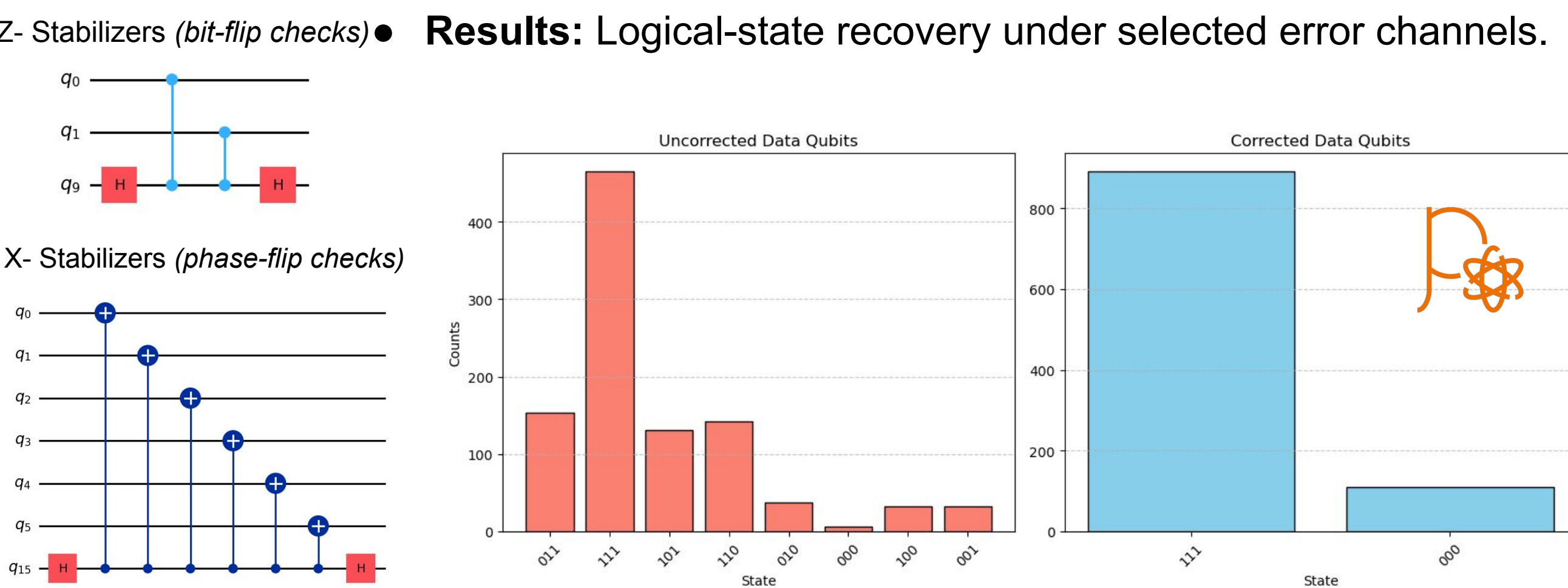
- Motivations:** Quantum computers are highly sensitive to noise and decoherence, making error reduction essential for reliable quantum computation.
- This project explores **error suppression, error mitigation, and error correction techniques** using Amazon Braket and AWS computational resources, demonstrating practical workflows for scalable quantum simulations and quantum hardware interfacing.



## Error Correction

### Shor Code Simulation

- Concept:** 9-qubit stabilizer code protecting one logical qubit from single-qubit errors: *bit-flip*, *phase-flip*, and *both*. Stabilizer measurements detect errors. The circuit uses 9 data qubits and 8 ancilla qubits.
- Workflow:** State preparation, concatenated encoding, error injection, 8 stabilizer syndrome measurements, density-matrix simulation, and classical decoding.
- Tools:** Amazon Braket with the DM1.
- Results:** Logical-state recovery under selected error channels.



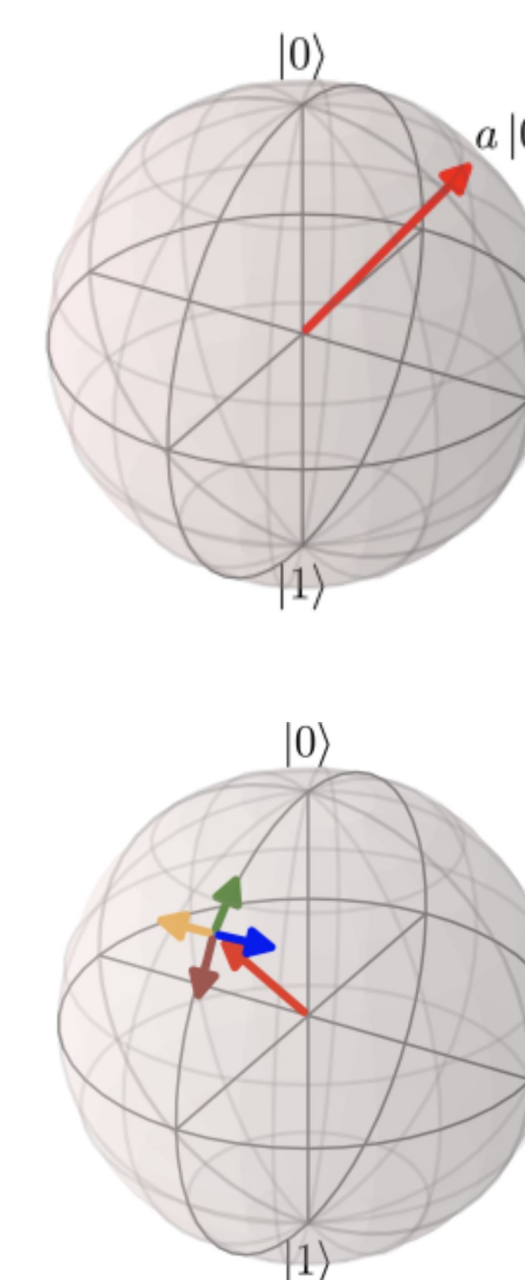
### Surface Code Simulation

- Concept:** Hardware-efficient code using local X- and Z-type stabilizers on a 2D lattice. Scalability is achieved via nearest-neighbor (NN) interactions that simplify hardware routing. Errors are detected as syndrome defects and decoded by matching.
- Workflow:** Stabilizer circuits, repeated syndrome extraction, and classical decoding.
- Tools:** *Stim* for fast stabilizer simulation, *PyMatching* for decoding, and AWS PCS for parallel HPC runs.
- Results:** increasing the code distance ( $d$ ) suppresses the logical error rate when the physical error rate is below the threshold.

## Error Suppression

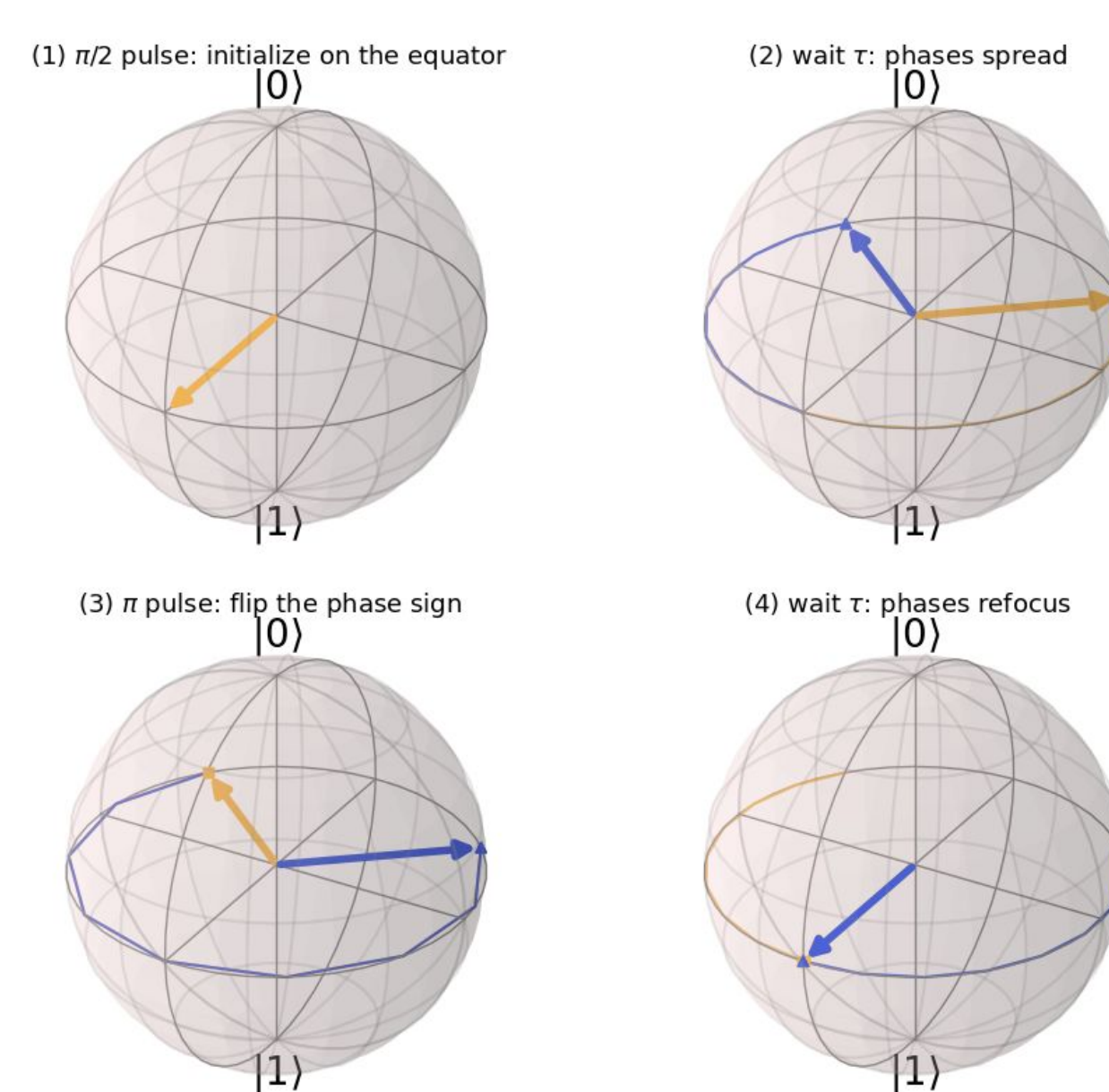
### Qubit characterization: $T_1$ , $T_2$ and $T_2^*$

- $T_1$ ,  $T_2$  and  $T_2^*$  are key timescales that describe how long a physical qubit can preserve quantum information
- $T_1$  measures how long a qubit can remain in  $|0\rangle$  or  $|1\rangle$  before energy relaxation changes its state
- $T_2$  and  $T_2^*$  measure how long a qubit preserves the relative phase of a superposition.  $T_2^*$  includes intrinsic dephasing plus slow frequency noise.  $T_2$  is the intrinsic dephasing time measured after refocusing the slow noise.

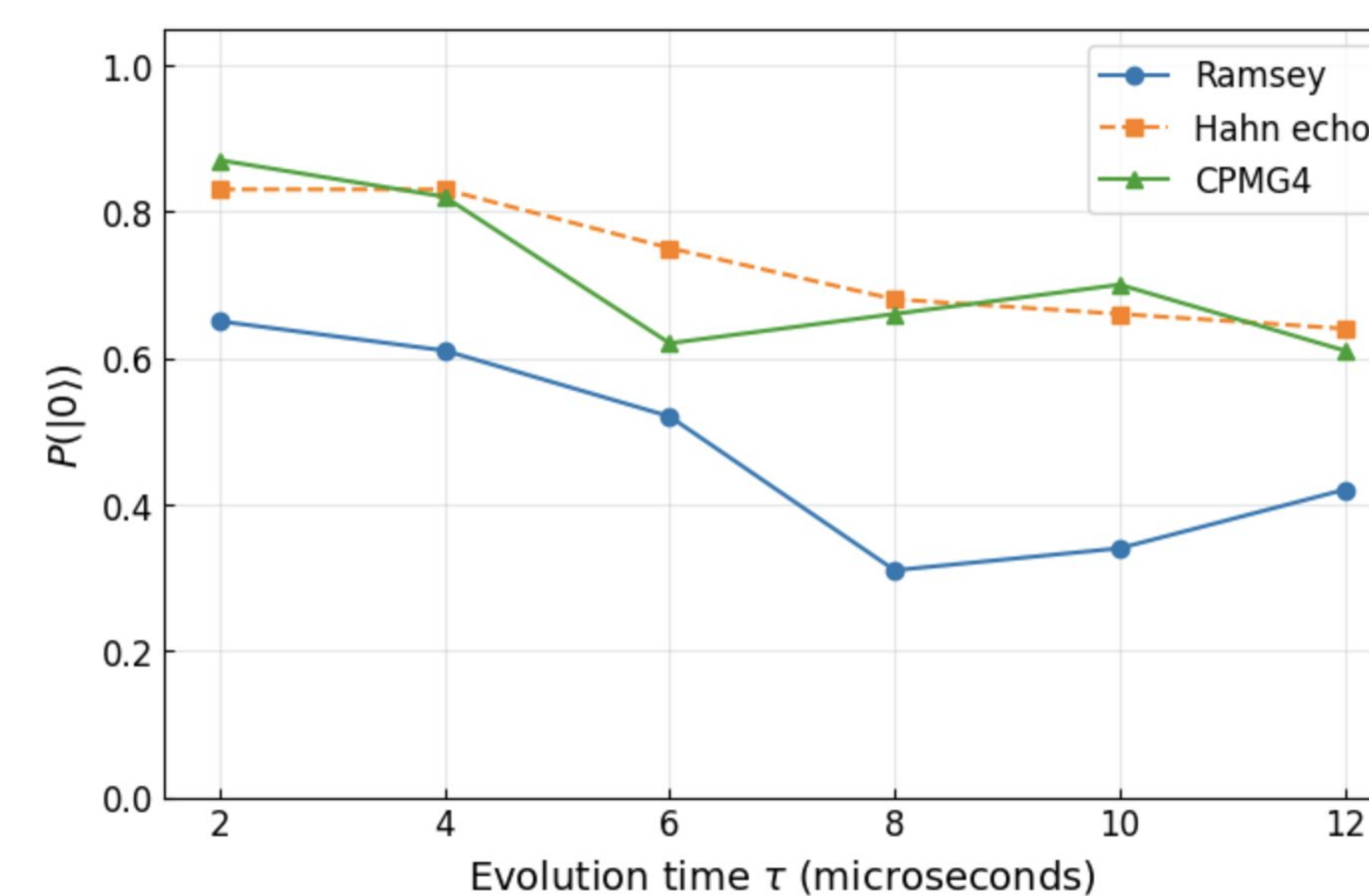


### Error suppression on the hardware level: dynamical decoupling

- Method:** Apply a sequence of control pulses to cancel part of the slow environmental noise.
- Commonly used sequences:** Hahn echo and Carr-Purcell-Meiboom-Gill (CPMG)



Pulse sequence of Hahn echo

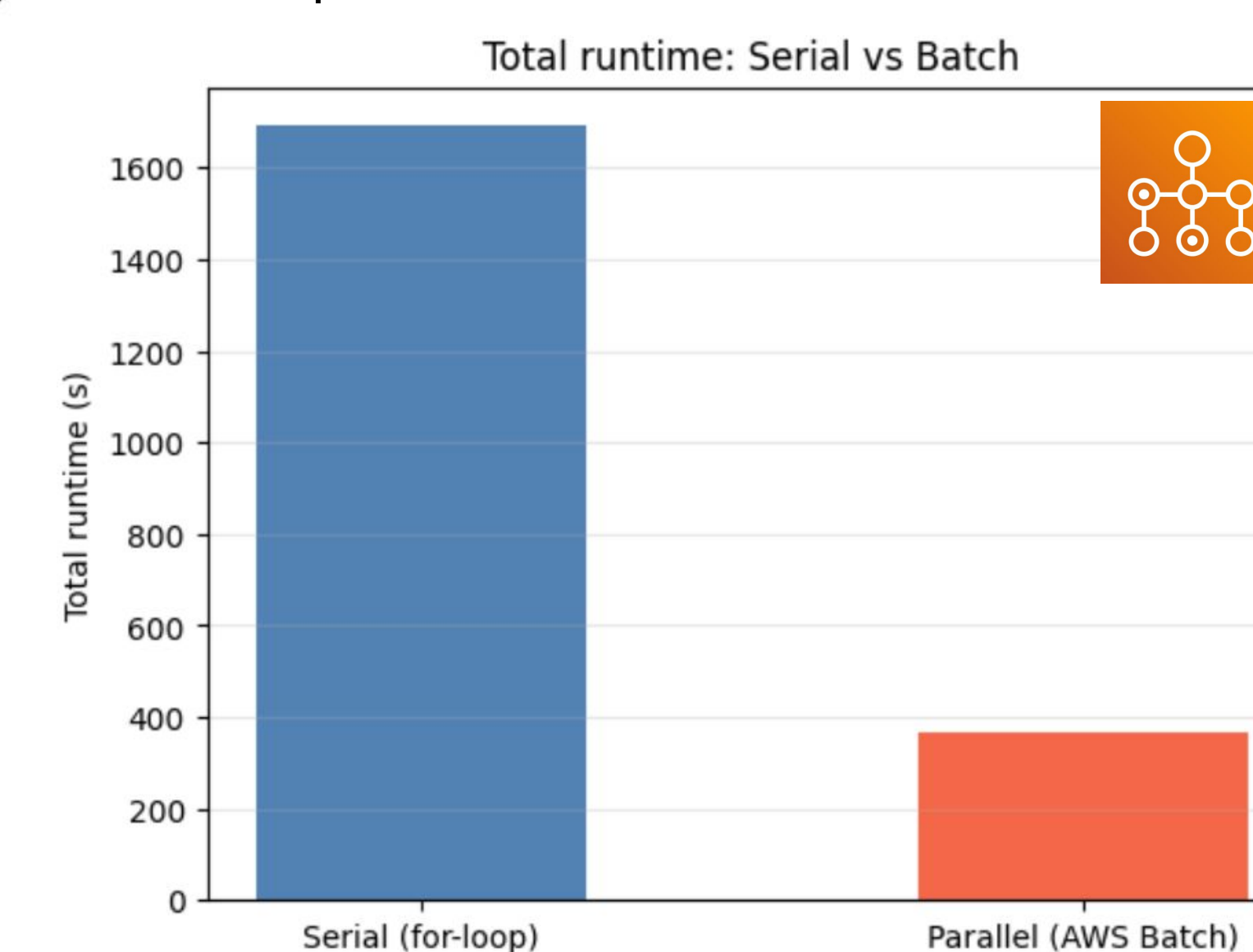
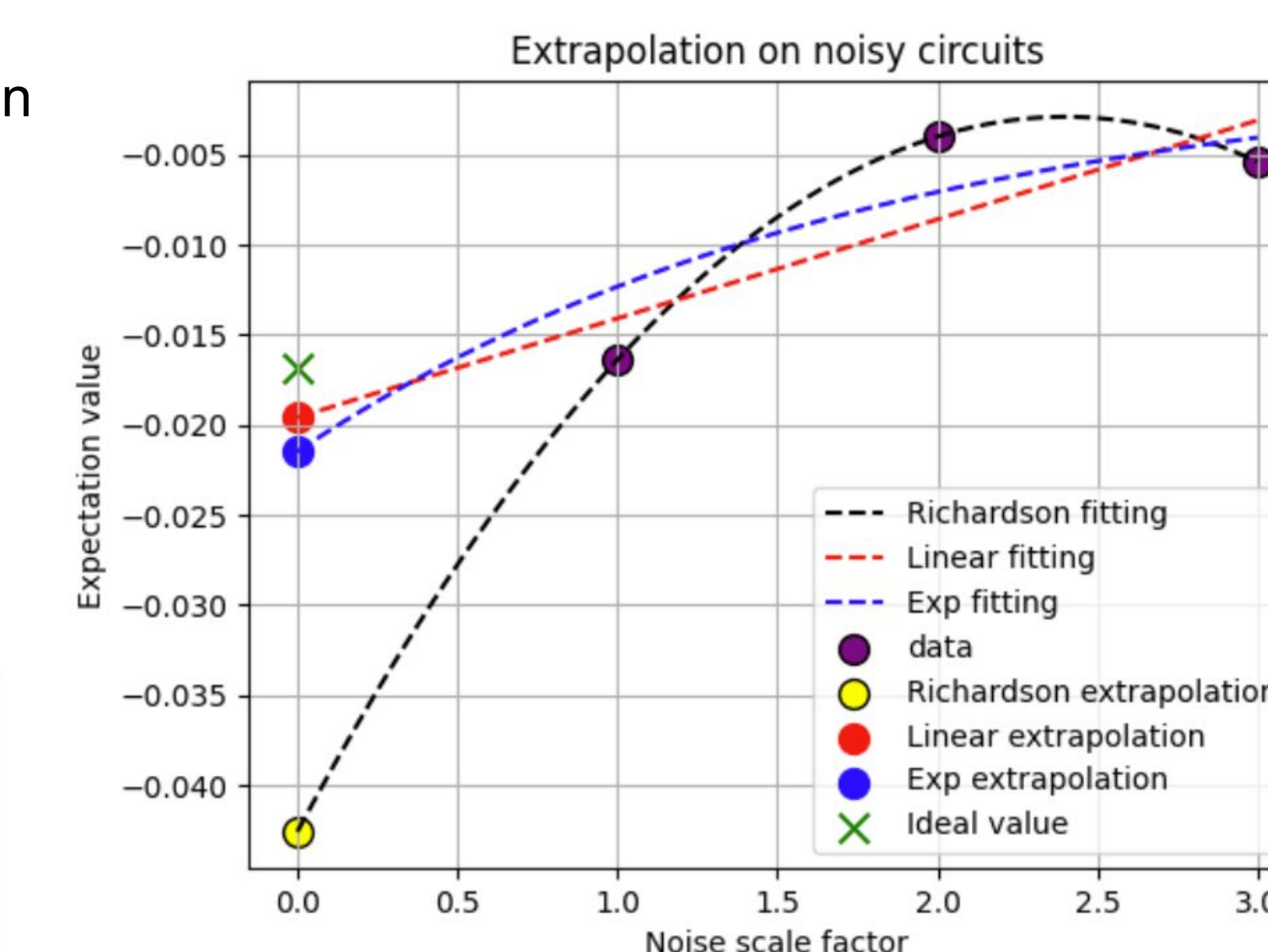
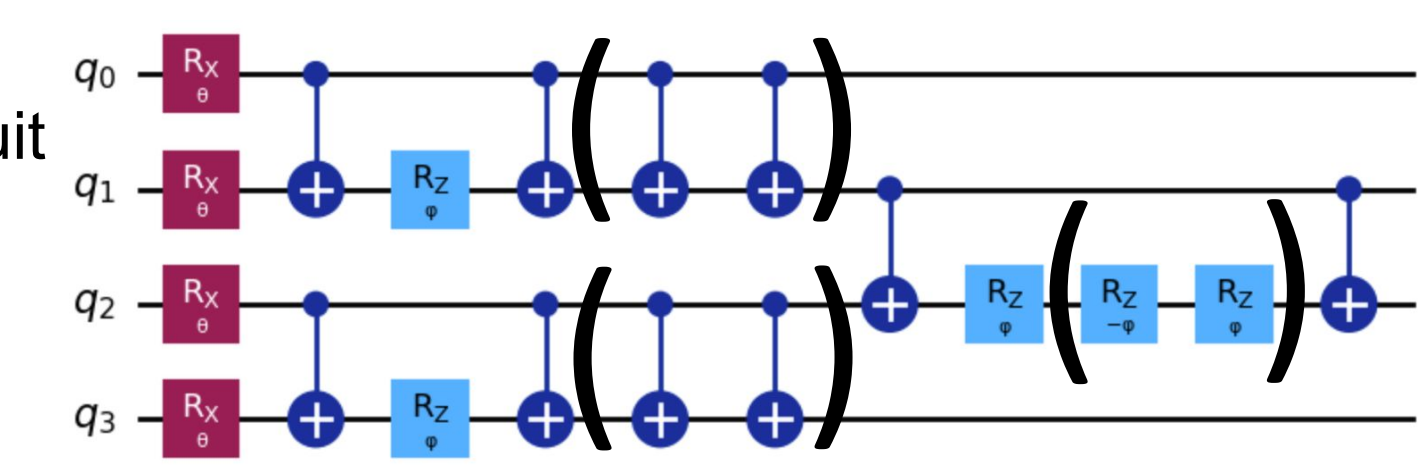


- Result:** Hahn echo and CPMG maintain a higher  $|0\rangle$  population than Ramsey at long evolution times. This shows that dynamical decoupling suppresses slow dephasing noise and helps preserve qubit coherence.

## Error Mitigation

### Zero-Noise Extrapolation

- Concept:** Extrapolate the ideal quantum circuit performance from outcomes of the scaled noise circuits.
- Workflow:** Build up circuits for ideal and scaled-noise 1D Ising model simulations. Extrapolate the results through the expectation values of the scaled-noise circuits.
- Tools:** Amazon Braket with the DM1 density-matrix simulator.
- Results:** Demonstrates zero-noise extrapolation with different methods and compare to the ideal values.



### AWS Batch

- Theory/Tools:** Get access to AWS Batch computation resources to accelerate the simulations.
- Workflow:** Build up circuits for each discrete time steps and upload to Batch. Retrieve data.
- Results:** Save 75% of the time for simulations with AWS Batch on heavy loading tasks.

## Summary

- We implemented and analyzed **dynamical decoupling, zero-noise extrapolation**, and quantum error correction protocols including **the Shor and surface codes**.
- Our results demonstrate improved coherence recovery, reduced simulation error, and logical error suppression below the fault-tolerance threshold.
- This work also highlights how Amazon Braket integrates quantum hardware, simulators, and scalable cloud resources for quantum computing research and education.

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